MLM for Experimental Data

PSYC 575

September 15, 2020 (updated: 2 October 2021)

Experimental Designs

- Within-subjects/mixed designs
 - Random assignment at level 1
- Between-subjects
 - Cluster-randomized trial
 - Treatment at level 2
 - Multisite trial
 - Treatment at level 1
 - See example in chapter 11 of Snijders and Bosker (2012)

Learning Objectives

- Identify the correct levels with experimental studies
- Describe designs with crossed random levels
- Assign variables to appropriate levels
 - And tell which variables can have random slopes at which levels
- Compute effect sizes (*R*²) for experimental data

Changes in Driving Scenes

- Example 1 from Hoffman & Rovine (2007)
 - Originally from Hoffman & Atchley (2001)
- Flicker paradigm: https://coglab.cengage.com/labs/change_detection.shtml

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Changes in Driving Scenes

• 153 persons

- Younger (*n* = 96), *M*_{age} = 19.7 years (*SD* = 2.3);
- Older (*n* = 57), *M*_{age} = 75.7 years (*SD* = 5.4)
- 51 scenes/items
 - Meaningfulness (0-5): meaningfulness to driving of the change
 - Salience (0-5): how visually conspicuous the change was within the scene
- Original plan: 2 (age group) × 2 (meaning) × 2 (salience) splitplot ANOVA

Data

- While RM-ANOVA uses the wide format, MLM requires the long format
 - Each unique response is in its own row
- See RStudio

Issues With ANOVA

- Unbalanced data/Missing responses
 - NA when change not detected within 60s
 - ANOVA uses listwise deletion: individual record is discarded when an individual has 1+ missing response

Issues of ANOVA

- ANOVA may require discretization of meaning and salience
- E.g., 0-2 for low salience, 3-5 for high salience
 - May hurt statistical power

What is the Data Structure?

- Each response represents a person answering an item
- Responses nested within persons?
- Responses nested within items?

Crossed Levels

Crossed Levels

• Cross-classified model



Crossed Levels at Level 2



Pre-Processing

• Log transformation of response time



Unconditional Model

- Repeated Measure (Within-cell) level (Lv 1)
 - $\lg_{i(j, k)} = \beta_{0(j, k)} + e_{ijk}$
- Between-cell (Person × Item) level
 - $\beta_{0(j,k)} = \gamma_{00} + u_{0j} + v_{0k}$

Intraclass Correlation

• Person level (Lv 2a) random effect: $u_{0j} \sim N(0, \tau_{u_0}^2)$

• ICC(person) =
$$\frac{\tau_{u_0}^2}{\tau_{u_0}^2 + \tau_{v_0}^2 + \sigma^2}$$

• Item level (Lv 2b) random effect: $v_{0k} \sim N(0, \tau_{v_0}^2)$

• ICC(item) =
$$\frac{\tau_{\nu_0}^2}{\tau_{u_0}^2 + \tau_{\nu_0}^2 + \sigma^2}$$

• ICC(person + item) =
$$\frac{\tau_{u_0}^2 + \tau_{v_0}^2}{\tau_{u_0}^2 + \tau_{v_0}^2 + \sigma^2}$$

Intraclass Correlation

Formula: lg_rt ~ (1 | id) + (1 | Item)
Random effects:

 ##
 Groups
 Name
 Variance
 Std.Dev.

 ##
 id
 (Intercept)
 0.1803
 0.4246

 ##
 Item
 (Intercept)
 0.1259
 0.3549

 ##
 Residual
 0.3899
 0.6244

Number of obs: 7646, groups: id, 153; Item, 51

- ICC(person) = 0.26
- ICC(item) = 0.18
- ICC(person + item) = 0.44

Varying Slopes With Crossed Levels

Rule for Random Slopes

 A predictor can have random slopes at a level above or at a crossed level



Varying Slopes Across Persons

- Repeated Measure level (Lv 1)
 - $\lg_{i(j, k)} = \beta_{0(j, k)} + e_{ijk}$
- Between-cell (Person × Item) level
 - $\beta_{0(j,k)} = \gamma_{00} + \beta_{1j} \operatorname{meaning}_k + u_{0j} + v_{0k}$
- Person level (Lv 2a)
 - $\beta_{1j} = \gamma_{10} + u_{1j}$

Any predictors at the repeated measure level or at the item level can have random slopes across persons

Varying Slopes Across Items

- Repeated Measure level (Lv 1)
 - $\lg_{i(j, k)} = \beta_{0(j, k)} + e_{ijk}$
- Between-cell (Person × Item) level
 - $\beta_{0(j,k)} = \gamma_{00} + \beta_{4k} \text{ oldage}_{j} + u_{0j} + v_{0k}$
- Item level (Lv 2b)
 - $\beta_{4k} = \gamma_{40} + V_{4k}$

Any predictors at the repeated measure level or at the person level can have random slopes across items

Hypothesized Model

- Repeated Measure level (Lv 1)
 - $\lg_{i(j, k)} = \beta_{0(j, k)} + e_{ijk}$
- Between-cell (Person × Item) level
 - $\beta_{0(j,k)} = \gamma_{00} + \beta_{1j} \operatorname{meaning}_k + \beta_{2j} \operatorname{salience}_k + \beta_{3j} \operatorname{meaning}_k \times \operatorname{salience}_k + \beta_{4k} \operatorname{oldage}_j + u_{0j} + v_{0k}$
- Person level (Lv 2a) random slopes
 - $\beta_{1j} = \gamma_{10} + \gamma_{11} \text{ oldage}_j + u_{1j}$
 - $\beta_{2j} = \gamma_{20} + \gamma_{21} \text{ oldage}_j + u_{2j}$
 - $\beta_{3j} = \gamma_{30} + \gamma_{31} \text{ oldage}_j + u_{3j}$

Hypothesized Model

- Item level (Lv 2b) random slopes
 - $\beta_{4k} = \gamma_{40} + v_{4k}$



Notes

- Because of counterbalancing
 - Person-level variables have no item-level variance
 - Item-level variables have no person-level variance
- Therefore, no need for cluster-mean centering

```
Formula: c_sal ~ (1 | id)
   Data: driving_dat
REML criterion at convergence:
23545.51
Random effects:
Groups Name Std.Dev.
id (Intercept) 0.000
Residual 1.094
```

Notes

- To more easily interpret the interactions, we want to grandmean center meaning and salience
 - They were centered to 3.0 in the data

Notes

- By testing random slopes one by one, the final model includes
 - Random slopes of c_sal (across persons)
 - Random slopes of oldage (across items)
- All two-way and three-way interactions were found not significant

Three-Way Interaction Plot

Predicted values of Natural Log RT in Seconds



Effect Size

See R Code