## Review of Regression Analysis

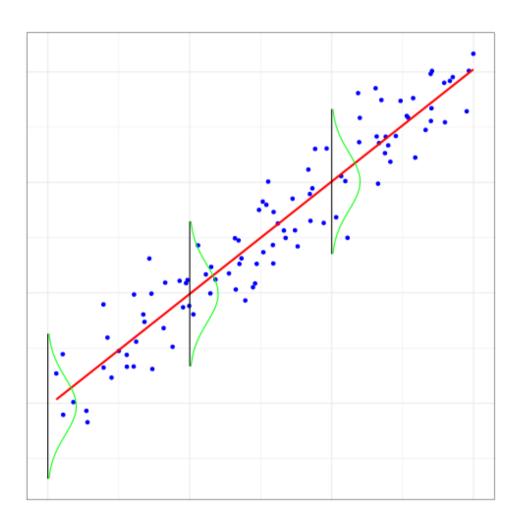
### **PSYC 575**

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### Statistical Model



# A set of statistical assumptions describing how data are generated

• Deterministic/fixed component

 $Y_i=eta_0+eta_1X_{1i}+eta_2X_{2i}+\dots$ 

• Stochastic/random component

 $egin{aligned} Y_i &= eta_0 + eta_1 X_{1i} + eta_2 X_{2i} + \ldots + eta_i \ & eta_i \sim N(0,\sigma) \end{aligned}$ 

### Why Regression?

MLM is an extension of multiple regression to deal with data from multiple levels

### Learning Objectives

#### Refresh your memory on regression

- Describe the statistical model
- Write out the model equations
- Simulate data based on a regression model
- Plot interactions

### **R** Demonstration

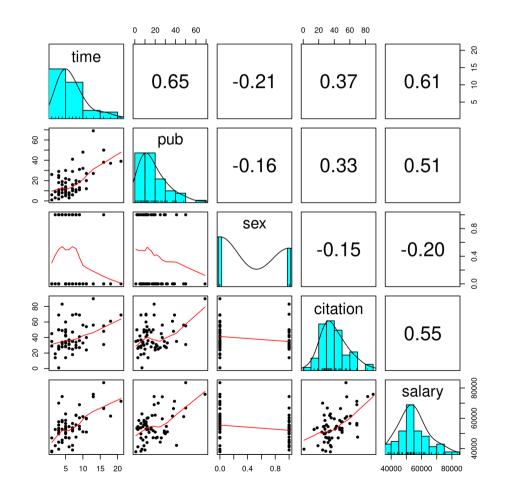
### Salary Data

#### From Cohen, Cohen, West & Aiken (2003)

Examine factors related to annual salary of faculty in a university department

- time = years after receiving degree
- pub = # of publications
- sex = gender (0 = male, 1 = female)
- citation = # of citations
- salary = annual salary

### Data Exploration



- How does the distribution of salary look?
- Are there more males or females in the data?
- How would you describe the relationship between number of publications and salary?

### Simple Linear Regression

Sample regression line

**Confidence intervals** 

Centering

### Simulation

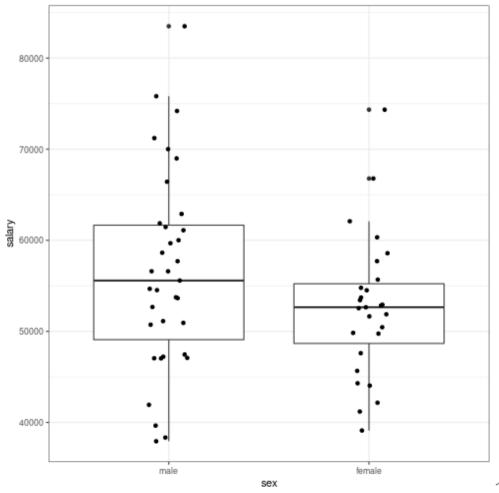
See lecture and R code

### **Categorical Predictors**

#### Dummy Coding

With k categories, one needs k-1 dummy variables

The coefficients are differences relative to the reference group



### **Categorical Predictors**

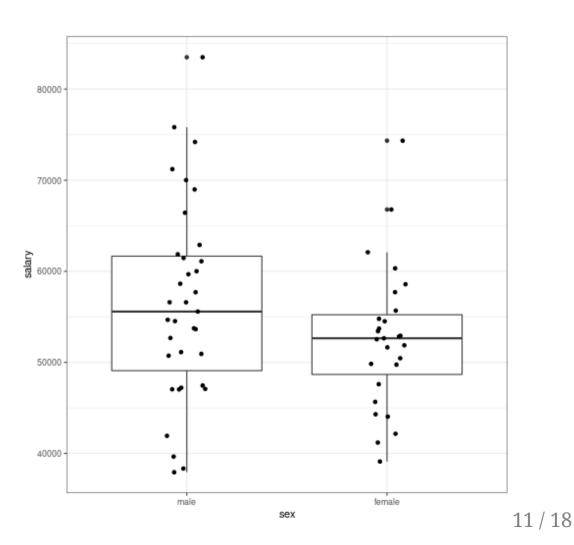
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Male = 0

 $y=eta_0+eta_1(0)=eta_0$ 



### **Categorical Predictors**

#### Dummy Coding

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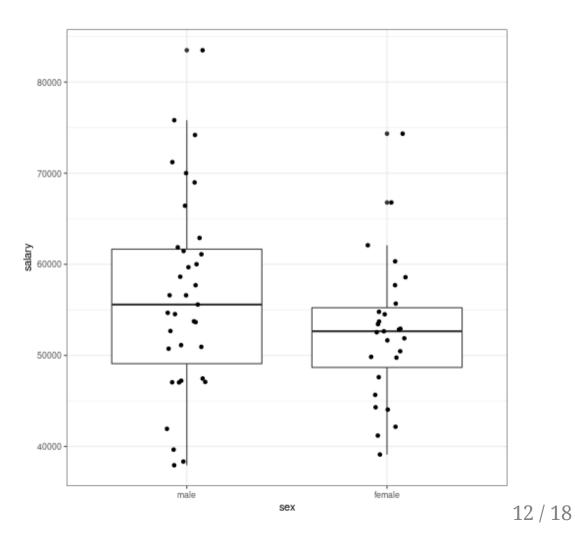
The coefficients are differences relative to the reference group

Male = 0

$$y=eta_0+eta_1(0)=eta_0$$

Female = 1

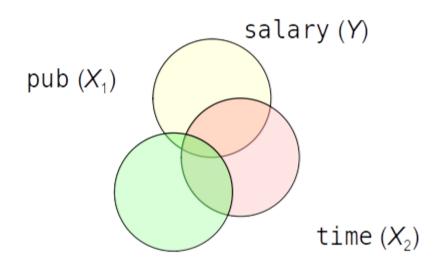
$$y=eta_0+eta_1(1)=eta_0+eta_1$$



### Multiple Regression

### Partial Effects

$$ext{salary}_i = eta_0 + eta_1 ext{pub}_i^c + eta_2 ext{time}_i + e_i$$



### Interpretations

Every unit increase in X is associated with  $\beta_1$  unit increase in Y, when all other predictors are constant

### Interactions

Regression slope of a predictor depends on another predictor

 $\widehat{ ext{salary}} = 54238 + 105 imes ext{pub}^c + 964 imes ext{time}^c + 15( ext{pub}^c)( ext{time}^c)$ 

 $\texttt{time} = 7 \Rightarrow \texttt{time}_\texttt{c} = 0.21$ 

$$\widehat{ ext{salary}} = 54238 + 105 imes ext{pub}^c + 964(0.21) \ + 15( ext{pub}^c)(0.21) \ = 54440 + 120 imes ext{pub}^c$$

 $\texttt{time} = 15 \Rightarrow \texttt{time}_\texttt{c} = 8.21$ 

$$\widehat{ ext{salary}} = 54238 + 105 imes ext{pub}^c + 964(8.21) \ + 15( ext{pub}^c)(8.21) \ = 62152 + 228 imes ext{pub}^c$$

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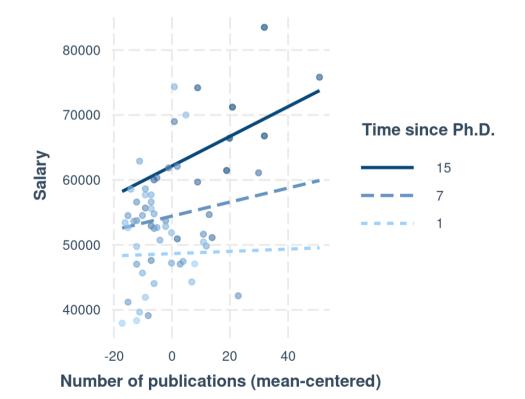
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### modelsummary::msummary()

```
library(modelsummary)
msummary(list("M3 + Interaction" = m4),
        fmt = "%.1f") # keep one digit
```

	M3 + Interaction
(Intercept)	54238.1
	(1183.0)
pub_c	104.7
	(98.4)
time_c	964.2
	(339.7)
pub_c × time_c	15.1
	(17.3)
Num.Obs.	62
R2	0.399
R2 Adj.	0.368
AIC	1291.8
BIC	1302.4

### Summary

#### Concepts

- What is a statistical model
- Linear/Multiple Regression
  - Centering
  - Categorical predictor
  - Interpretations
  - Interactions

#### HW 2

Try replicating the examples in the Rmd file